

Day 3 - Introduction to limits

On the paper, describe your experience  
w/ accessing the online PDFs.

→ Name

→ did you try?

if yes → how did it go?

if no → why not?

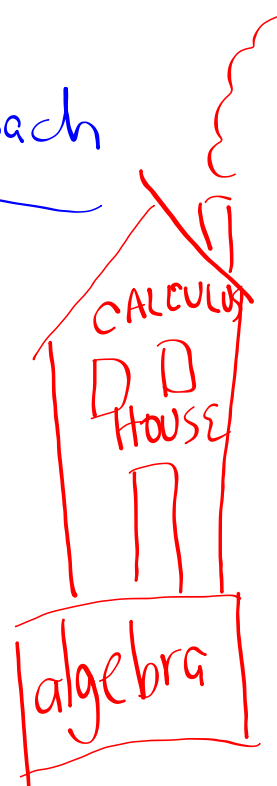
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LimitsInductive approach

figure  
out  
based  
on #'s  
or pictures

Deductive approach

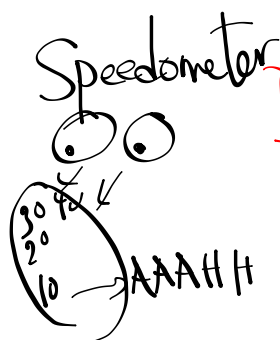
be sure  
→  
⇒ algebra



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# MOTIVATION

$$\text{DISTANCE} = \text{RATE} \times \text{DURATION}$$



Instantaneous  
Velocity

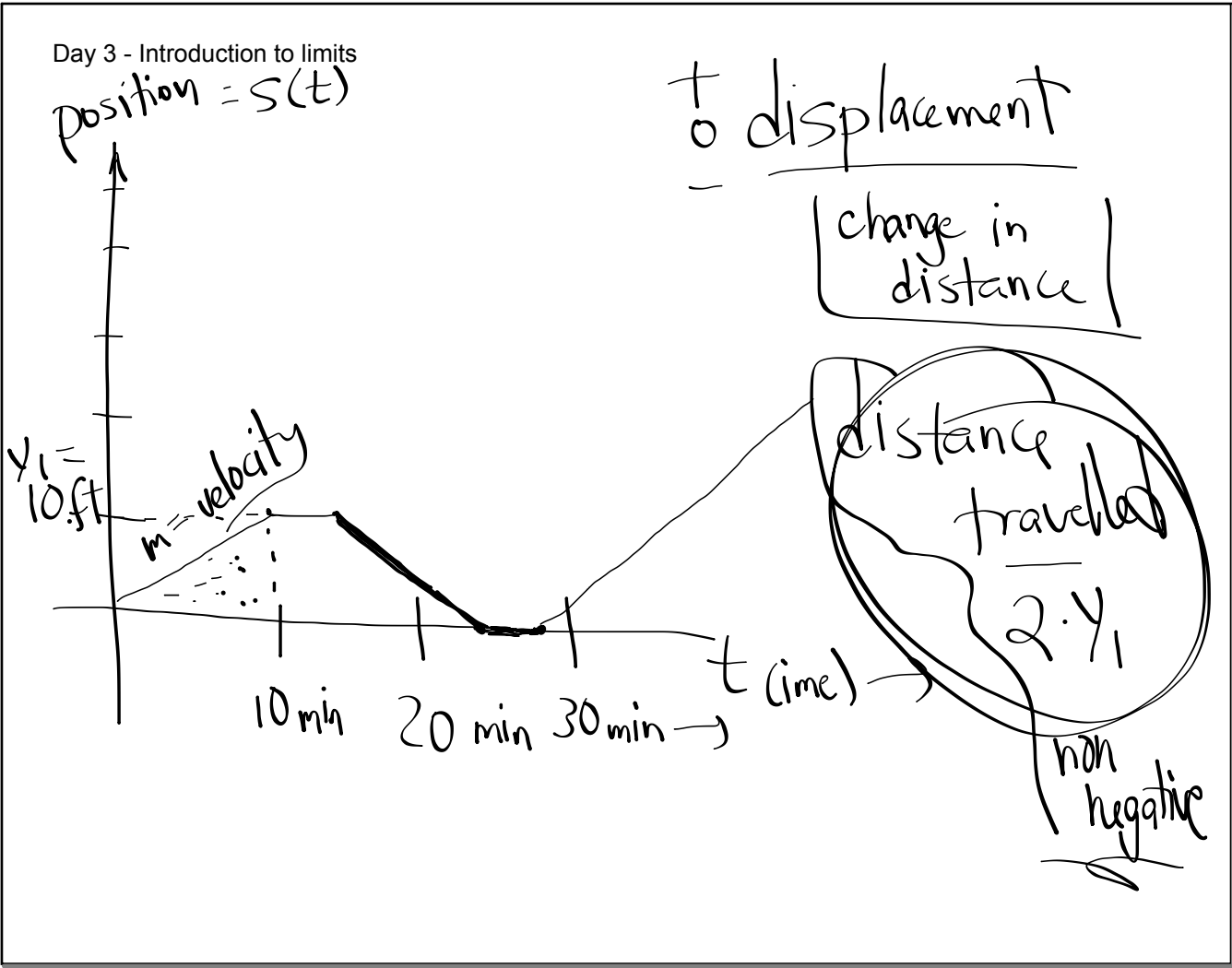
$$\frac{\text{DISTANCE}}{\text{DURATION}} = \text{RATE}$$

AVERAGE  
VELOCITY

$\frac{+}{-} \frac{0}{\infty}$  SPEED

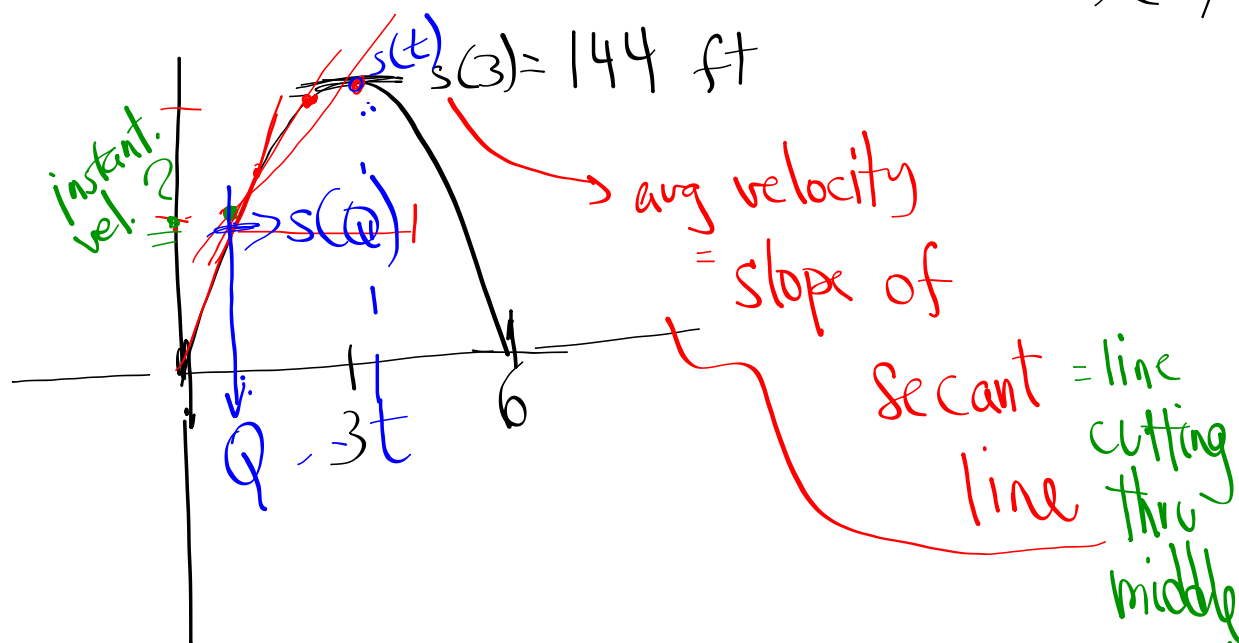
VS

$\frac{+}{-} \frac{0}{\infty}$  VELOCITY



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Ex 1.  $s(t) = -16t^2 + 96t = (6-t)(16t)$



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The instantaneous velocity of a blob whose pos<sup>n</sup> is given by  $s(t)$ , at time =  $Q$

$$\text{is : } \lim_{t \rightarrow Q} \frac{s(t) - s(Q)}{t - Q}$$

inst vel      avg vel

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$$s(t) = -16t^2 + 96t$$

$$y_1 = -16x^2 + 96x$$

$$\begin{aligned} \text{avg vel} &= \\ \frac{144-128}{3-2} & \\ &= 16 \frac{\text{ft}}{\text{sec}} \end{aligned}$$

$$s(2) = 128 \text{ ft}$$

$$s(3) = 144 \text{ ft}$$

$$s(1) = 80 \text{ ft}$$

$$\begin{aligned} \text{avg vel} & \\ \text{fr } t=1 \text{ to } 2 & \end{aligned}$$

$$= \frac{128-80}{2-1} = 48 \frac{\text{ft}}{\text{sec}}$$

$$y_1(3)$$

VARs

→

"FUNCTION"

$$\begin{aligned} y_1 \\ y_2 \\ y_3 \\ \vdots \end{aligned}$$

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$$s(t) = -16t^2 + 96t$$

$$\text{inst vel @ } t=2 = \lim_{t \rightarrow 2} \frac{s(t) - s(2)}{t - 2} = \lim_{t \rightarrow 2} \frac{(-16t^2 + 96t) - (-128)}{t - 2}$$

CANCEL  
OUT  
ZEROS

$$= \lim_{t \rightarrow 2} \frac{-16(t^2 - 6t + 8)}{t - 2}$$

$$= \lim_{t \rightarrow 2} \frac{-16(t-2)(t-4)}{t-2}$$

$$= \lim_{t \rightarrow 2} \frac{-16(t-4)}{1} = -16(2-4) = +32 \frac{\text{ft}}{\text{sec}}$$



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Hw read ch 2, section 1 and 2 (online)  
2.1 / 1-33 odd  
(by 4s)



ans: . . . . . / ANS-CO2 .pdf  
/ CO2\_sol.pdf

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